NAG Fortran Library Routine Document

F06SJF (ZTRSV)

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

F06SJF (ZTRSV) performs one of the matrix-vector operations

$$x \leftarrow A^{-1}x, \quad x \leftarrow A^{-T}x \quad \text{or} \quad x \leftarrow A^{-H}x,$$

where A is an n by n complex triangular matrix, and x is an n element complex vector. A^{-T} denotes $\left(A^T\right)^{-1}$ or equivalently $\left(A^{-1}\right)^T$; A^{-H} denotes $\left(A^H\right)^{-1}$ or equivalently $\left(A^{-1}\right)^H$.

No test for singularity or near-singularity of A is included in this routine. Such tests must be performed before calling this routine.

2 Specification

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SUBROUTINE F06SJF (UPLO, TRANS, DIAG, N, A, LDA, X, INCX)

INTEGER           N, LDA, INCX
complex*16        A(LDA,*), X(*)
CHARACTER*1       UPLO, TRANS, DIAG
```

The routine may be called by its BLAS name **ztrsv**.

3 Description

None.

4 References

None.

5 Parameters

1:   UPLO – CHARACTER*1   *Input*

On entry: specifies whether A is upper or lower triangular as follows:

      if UPLO = 'U', A is upper triangular;
      if UPLO = 'L', A is lower triangular.

Constraint: UPLO = 'U' or 'L'.

2:   TRANS – CHARACTER*1   *Input*

On entry: specifies the operation to be performed as follows:

      if TRANS = 'N', $x \leftarrow A^{-1}x$;
      if TRANS = 'T', $x \leftarrow A^{-T}x$;
      if TRANS = 'C', $x \leftarrow A^{-H}x$.

Constraint: TRANS = 'N', 'T' or 'C'.

3:     DIAG – CHARACTER*1   *Input*

On entry: specifies whether A has non-unit or unit diagonal elements, as follows:

> if DIAG = 'N', the diagonal elements are stored explicitly;
> if DIAG = 'U', the diagonal elements are assumed to be 1, and are not referenced.

Constraint: DIAG = 'N' or 'U'.

4:     N – INTEGER   *Input*

On entry: n, the order of the matrix A.

Constraint: N $\geq$ 0.

5:     A(LDA,∗) – *complex*16* array   *Input*

Note: the second dimension of the array A must be at least $\max(1, N)$.

On entry: the n by n triangular matrix A. If UPLO = 'U', A is upper triangular and the elements of the array below the diagonal are not referenced; if UPLO = 'L', A is lower triangular and the elements of the array above the diagonal are not referenced. If DIAG = 'U', the diagonal elements of A are not referenced, but are assumed to be 1.

6:     LDA – INTEGER   *Input*

On entry: the first dimension of the array A as declared in the (sub)program from which F06SJF (ZTRSV) is called.

Constraint: LDA $\geq \max(1, N)$.

7:     X(∗) – *complex*16* array   Input/Output

On entry: the vector x.

On exit: the updated vector x.

8:     INCX – INTEGER   *Input*

On entry: the increment in the subscripts of X between successive elements of x.

Constraint: INCX $\neq$ 0.

6   Error Indicators and Warnings

None.